

Segregated by Design? Street Network Topological Structure and the Measurement of Urban Segregation*

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Racial residential segregation is a longstanding topic of focus across the disciplines of urban social science. Classically, segregation indices are calculated based on areal groupings (e.g. counties or census tracts), with more recent research exploring ways that spatial relationships can enter the equation. Spatial segregation measures embody the notion that proximity to one's neighbors is a better specification of residential segregation than simply who resides together inside the same arbitrarily-drawn polygon. Thus, they expand the notion of "who is nearby" to include those who are geographically close to each polygon rather than a binary inside/outside distinction. Yet spatial segregation indices often resort to crude measurements of proximity, such as the Euclidean distance between observations, given the complexity and data requirements of calculating more theoretically-appropriate measures, such as distance along the pedestrian travel network. In this paper, we examine the ramifications of such decisions. For each metropolitan region in the U.S., we compute both Euclidean and network-based spatial segregation indices. We use a novel inferential framework to examine the statistical significance of the difference between the two measures and following, we use features of the network topology (e.g. connectivity, circuitry, throughput) to explain this difference using a series of regression models. We show that there is often a large difference between segregation indices when measured by these two strategies (which is frequently significant). Further, we explain which topology measures reduce the observed gap and discuss implications for urban planning and design paradigms.

Keywords: segregation, neighborhoods, spatial analysis, network analysis, spatial weights

INTRODUCTION

An exceedingly common abstraction in applied spatial analysis is the use of Euclidean distance as a proxy measure for geographic proximity (which is, itself, often a proxy for the frequency of social interaction). It is the geographical scientist's equivalent to the physicist's spherical cow¹, or the economist's perfect market: a useful abstraction that helps partially explain a much more complex underlying process, however imperfectly. A major difference in spatial analysis, however, is that scientists from many disciplines often fail to realize how simplified the assumption of Euclidean distance is when traversing the built or natural environment. While, in general, simple proximity is a reasonable heuristic for understanding Tobler's Law (Tobler 1970), the behavioral realities of movement and social interaction in complex urban environments often require a more thoughtful model.

More directly, cities, regions, and neighborhoods are not featureless planes in which agents have perfect freedom of mobility. Rather, they are multifaceted environments populated by highways, canyons, rivers, mountains, railroad tracks, alleyways, and power plants. To facilitate movement in this environment, an interleaved transportation system provides passageways through discrete locations, and conditions how easy it is to move throughout the region and interact with individuals in other parts of the region. Although pure Euclidean distance can proxy this system, the urban design

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¹https://en.wikipedia.org/wiki/Spherical_cow

decisions that govern how and where networks are located, as well as the natural features like elevation or water features play an important, albeit underexamined, role in mediating social interactions.

One particular topic where a full understanding of space would provide significant benefits is segregation analysis, a longstanding topic of focus across the disciplines of urban social science. Classically, segregation indices are calculated based on areal groupings (e.g. counties or census tracts), with more recent research exploring ways that spatial relationships can enter the equation. Spatial segregation measures embody the notion that proximity to one's neighbors is a better specification of residential segregation than simply who resides together inside the same arbitrarily-drawn polygon. Thus, they expand the notion of "who is nearby" to include those who are geographically close to each other rather than a binary inside/outside distinction. Yet spatial segregation measures often resort to crude measurements of proximity, such as the Euclidean distance between observations, given the complexity and data requirements of calculating more theoretically-appropriate measures, such as distance along the pedestrian travel network.

In this paper, we examine the relationship between pedestrian network characteristics and the measurement of metropolitan segregation. In doing so, we examine three research questions in turn: first, how much does the operationalization of space matter for segregation measurement? More specifically, how large is the difference between Euclidean-based and network-based measures of spatial segregation? Second, if differences exist between Euclidean and network measures, are they large enough that they cannot be attributed to chance? Third, what characteristics of the travel network are related to the observed difference in measurement? If there is a large and/or systematic difference between traditional spatial measurements and those leveraging more realistic measurements of distance, then there may be much to learn about the contribution of network structure and design when seeking to maximize urban integration.

Urban Infrastructure and Social Interactions

Since the inception of city planning, the relationship between social interactions and the built environment has been a topic of intense focus for both social scientists and urban designers (Talen 2017). The normative concepts of urban utopias prescribed by architects like Ebenezer Howard, Frank Lloyd Wright, and Le Corbusier included distinct visions for how densely populated and separated/integrated land uses could facilitate the ideal level of interaction between a resident and (a) her neighbors, and (b) her natural surroundings (Corbusier 1986, Campbell and Fainstein 1996, Howard and Osborn 2001). Combining these visions with ideas from Wirth (1938) and the famous 'neighborhood unit plan' articulated by Perry (1929), large scale developers like James Rouse developed concepts for New Towns like Columbia, Maryland that were based largely on the design of insular street networks (Olsen 2003).

At their best, these designs were intended to foster community for the residents that live within them, and ensure that amenities like school, shopping, employment, and leisure are all within a walkable distance from the neighborhood's core. From a more cynical perspective, the cul-de-sac patterns

and interspersed greenways of the ‘neighborhood unit plan’ helped codify the American ideal of white flight and the picturesque upper-middle class neighborhood, using both urban design and land-use policy as informal mechanisms of residential sorting. Thus, although the arrangement of people in space has been a focus of urban thought for more than a century, it remains an open question how well features of the real urban fabric are represented in quantitative models of social interaction, such as segregation indices—and whether urban design characteristics shape our perception of these patterns.

Now we have both the tools and the logic to test these assumptions and understand the role of abstractions such as Euclidean distance-based measures in our assessment of critical social processes such as residential segregation. Fast graph algorithms allow us to construct more realistic concepts of spatial weights matrices, and computational statistics allow us to construct and test realistic null hypotheses about the allocation of urban population groups. Here, we examine the role of street network topology in the appropriate measurement of urban segregation. Our goals are twofold.

First, we aim to understand the implications of simple Euclidean distance-based abstractions when conducting formal spatial analyses; that is, do we find substantive differences in results when more realistic concepts of spatial relationships (e.g. network connectivity) are considered? Second, we aim to explore the elements of urban design (particularly the street network configuration) in widening the gap between analytical abstraction and empirical reality. More simply, we aim to understand whether certain elements of the street network are associated with a greater difference in measured segregation. With this knowledge, urban designers and planners can begin with more inclusive communities from the beginning.

MEASURING SEGREGATION IN SPACE

Incorporating Distance into Segregation Indices

In a foundational contribution, White (1983) conceives of segregation in terms of spatial interaction, and formulates a spatial dissimilarity index using an exponential decay function to weight the proximity between observed census units. Despite the importance of the contribution, the application of White’s technique has never become widespread, perhaps in part because of the difficulty in operationalizing the index prior to modern GIS. Through the 1990s a surge of research on spatial segregation indices examined different methods for incorporating space, leveraging the growing GIS capacity of the era. An important critique of the time is given by Wong (1993) who shows that spatial segregation indices based on contiguity between adjacent units provide poor definitions of the local neighborhood. This criticism is based in part because geographic units are heterogeneously-sized and also because polygon adjacency may be a poor measurement of “nearness”. Additional work has explored the sensitivity of segregation measures to the modifiable areal unit problem (MAUP) (Openshaw 1984), and by extension, the importance of spatial scale (Wong 1997, Wong 2004). Some authors have also developed spatial extensions or decompositions of popular indices such as the Gini index

(Dawkins 2004, Rey and Folch 2011)

In a canonical contribution to the segregation literature, Reardon and O’Sullivan (2004) develop a generalized framework for creating spatial segregation indices using a generic formulation of the neighborhood. They also show that the spatial information theory index \tilde{H} and the spatial isolation/exposure index \tilde{P}^* have the most desirable conceptual and mathematical properties. O’Sullivan and Wong (2007) provide an operationalization of this approach using kernel density estimation to operationalize the notion of the neighborhood in continuous space, overcoming many of the traditional criticisms of spatial segregation measures. In doing so, they provided an important path forward for a body of work that has continued to expand the notion of space.

A variety of authors have also begun to examine the role of spatial scale. In an important advance in segregation methods, Reardon *et al.* (2008) develop a method for understanding the implications of multiscale segregation by varying the distance parameter used to compute the local environment in a spatial segregation index. Following, Reardon *et al.* (2009) and Lee *et al.* (2008) apply the framework to a large set of metropolitan regions in the U.S., demonstrating a wide variety of macro versus micro-scaled patterns, and other work has explored the role of multiscale change over time (Bailey 2012, Fowler 2016). Another prominent body of work builds on this work, exploring the notion of “egohoods,” where each household has its own concept of the neighborhood that extends outward and partially overlaps with others nearby (Hipp and Boessen 2013, Petrović *et al.* 2018, 2019). Even more recently, additional measurement techniques have been developed that help summarize multiscale patterns using a single index (as opposed to an array or a ratio) (Clark *et al.* 2015, Östh *et al.* 2015, Olteanu *et al.* 2019, Bézenac *et al.* 2022). This research has provided clear evidence not only of the importance of considering spatial relationships in segregation measurement, but also the ways that misspecification of space (such as application of an inappropriate scale) can lead to a skewed concept of the phenomenon under study.

Transportation and Social Interaction

Elsewhere, scholars have examined the role of physical barriers and built features of the urban environment in facilitating social contact. For example Grannis (2005) shows social interactions are more frequent inside “T-communities” defined by street networks (Grannis 2005), and Roberto (2018) uses street networks to measure segregation in a small-scale case study, and shows that segregation in Pittsburgh is higher when measured according to network distance. These contributions emphasize a long-recognized but understudied element of metropolitan segregation patterns, namely that transport networks, physical barriers, and other factors such as elevation or congestion condition the expected potential for social interaction in space. For example work in sociology has shown the importance of street network connectivity in fostering social networks inside small urban geographic zones (Grannis 1998). The natural logic underlying these findings is that street networks can help insulate urban environments and provide greater exposure to residents living inside “the neighborhood” than those who live outside, but this distinction can be masked easily when measuring metropolitan space

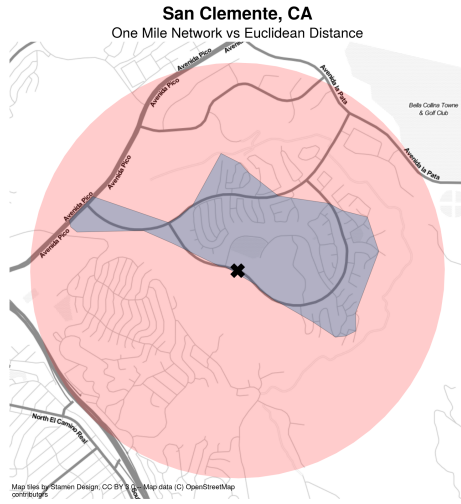
using Euclidean distances.

A depiction of the difference between network travel distance and “as the crow flies” distance is shown in Figure 1. The figure shows an origin marked with an X in the center, and two different polygons representing a one-mile travel distance using different methods in the cities of San Clemente and Chicago. The small polygon depicts the total extent accessible from the origin point when traveling along the pedestrian network, whereas the larger polygon depicts the 1-mile buffer representing unconstrained travel. It is immediately apparent in the figure that network-constrained travel covers a much smaller footprint than Euclidean distance in the depicted location. Furthermore, the pattern appears to be influenced strongly by the street network and urban design features that characterize the largely suburban region of San Clemente.

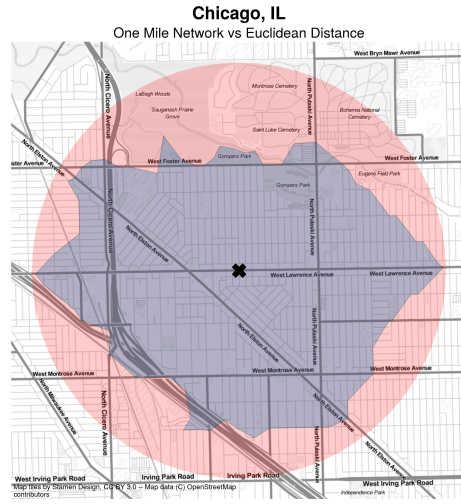
Instead of a regular grid that facilitates travel in all directions (like the densely urbanized section of Chicago in Figure 1b), the street network in Figure 1a includes several insular patterns, cul-de-sacs, and 3-way intersections that help channel traffic in certain directions rather than others. Furthermore, the fact that some subdivisions have only a single entrance makes clear how much further a person would need to travel to reach the homes in certain regions (versus how much easier they appear to be reached via the circular buffer). By contrast, the regular gridded pattern in Chicago in Figure 1b allows travel to flow in all directions. Because the origin starts on a street oriented East-West, the polygon covers essentially the entire circular buffer in that direction. The North-South direction is limited, however for two reasons, first, the traveler needs to reach a cross street before changing direction, and second the Kennedy expressway provides a man-made physical barrier that impedes travel in the southwestern direction, creating a hard edge in the inner polygon except along a single passageway. A similar phenomenon impedes traffic in the northward direction, as the network does not extend into Saint Luke Cemetery.

Using evidence from a case study in Pittsburgh, Roberto (2018, p. 28) argues that, “even small positive differences in the city-level results are meaningful and suggest that physical barriers facilitate greater separation between ethnoracial groups and higher levels of segregation.” We agree with the spirit of this assessment, however, we would extend and clarify that physical barriers themselves do not necessarily create greater separation between groups—although action by other parts of the urban system such as inequitable land use planning or racial steering by lenders or agents can (and does) interact with these barriers to create segregated real estate markets and phenomena such as one group living on the “other side of the tracks” (Roberto 2018).

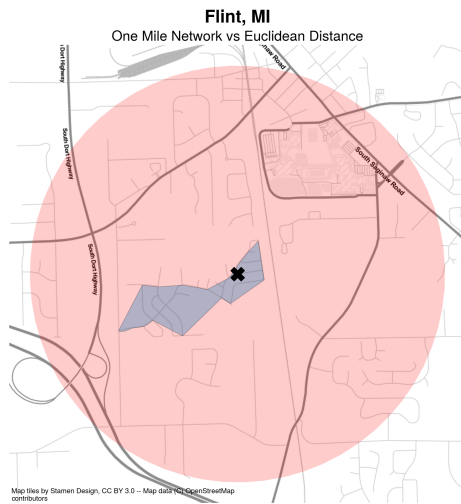
Further, as Figure 1 shows, it is not simply the presence of physical barriers, but also the geometric design and topological structure of the travel network that facilitates separation between people in urban space. The curvilinear, meandering streets, and abundance of cul-de-sacs in San Clemente stand in sharp contrast to the dense, regular grid in Chicago, even though the network in Chicago also includes additional barriers like highways. In what follows, we examine the magnitude of differences between network and simple Euclidean measures in detail for every metropolitan region in the United States. Specifically, we expand upon prior work in three different directions. First, we widen the geographic scope by considering every metropolitan region in the United States, rather than a case



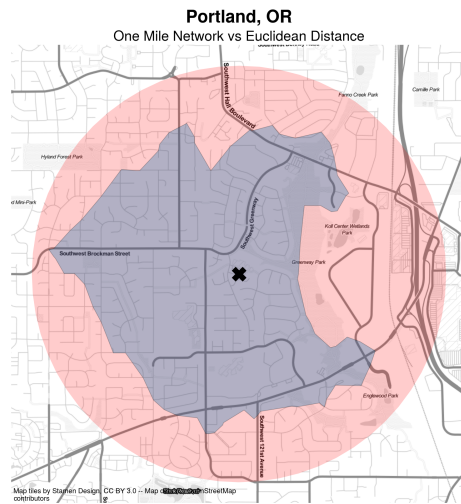
(a) Distance Comparison in San Clemente



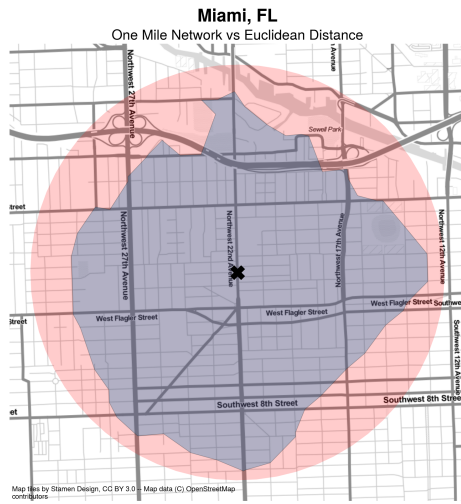
(b) Distance Comparison in Chicago



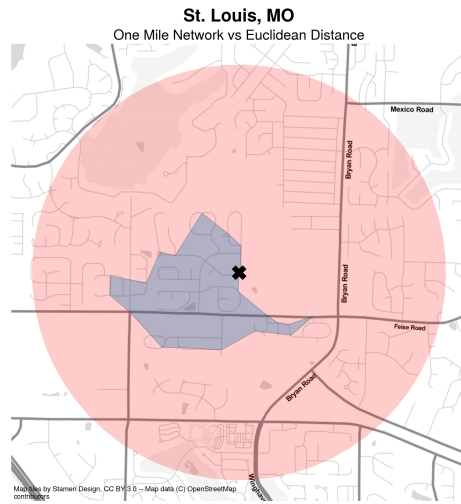
(c) Distance Comparison in Flint



(d) Distance Comparison in Portland



(e) Distance Comparison in Miami



(f) Distance Comparison in St Louis

Figure 1: Network Distance vs Euclidean Distance in Urban Environments

study of a single city. Second, we adopt a computational inference framework that allows us to assess whether the observed differences between the segregation measures are large enough that they could not happen by chance. Finally, we explore the relationship between differences in observed segregation and characteristics of the local travel network.

THE ROLE OF STREET NETWORKS IN SOCIAL SEPARATION

We begin our analysis by computing two sets of segregation indices, adopting the spatial information theory index \tilde{H} as our measure of segregation. As Reardon *et al.* (2008, p. 512) describe, “the index \tilde{H} is a measure of how much less diverse individuals’ local environments are, on average, than is the total population of region”, and reaches its maximum of 1 only when “each individual’s local environment is monoracial”. Here, our goal is to test how sensitive the statistic is to different concepts of the “local environment,” with one concept adopting the simplified assumption of Euclidean-based distance measurements, and the other requiring that distance be measured along a pedestrian transport network.

Computing Spatial Segregation Indices

Following Reardon and O’Sullivan (2004) we consider a spatial region populated by M racial groups indexed by m , with τ and π as population density and proportion, respectively. Here we diverge from the classical notation in the segregation literature and instead adopt conventions more common in spatial econometrics and geographic analysis.² Doing so allows us to strengthen the connection between similar concepts in different disciplines as well as gain finer control over the definition of spatial relationships. Since many spatial segregation measures are implemented in GIS and spatial analysis software designed by geographers, clarifying this connection can help ease interdisciplinary adoption and conversation around spatial segregation measures.

Thus, we index locations as i and j , and we operationalize the concept of spatial relationships using a spatial weights matrix W (Cliff and Ord 1970). By focusing on W , we are forced “to specify [our] underlying assumptions about socio-spatial proximity”, following the call by Reardon and O’Sullivan (2004, p. 154) for analysis that “compares segregation levels based on different theoretical bases for defining spatial proximity.” Conceptually, the spatial weights matrix W reflects the connectivity graph for the spatial relationship between nodes i and j , and the values w_{ij} encode the intensity of the association $\bar{i}\bar{j}$. The spatial weights matrix is a useful and flexible representation of the local neighborhood environment because it provides a generic data structure for encoding spatial relationships, where any link function (ϕ , following the notation of Reardon and O’Sullivan (2004)) can be used to specify the proximity between units. Formally,

²Notably, however, a similar notation is used by Grannis (2002) who defines the spatial weights matrix as C , in recognition of the common specification as a binary connectivity matrix. Despite this small change, Grannis also describes the applicability of other functions such as inverse-distance weighting.

$$W = \phi(D) \quad (1)$$

where ϕ is a proximity weighting function and D is a matrix containing pairwise distances for all i and j . Classically, W is typically created via binary connectivity between adjacent units, but a wide variety of other continuous specifications are also used in practice (Getis 2009, Rey and Anselin 2010, Halleck Vega and Elhorst 2015), such as the Euclidean distance between observations, or various kernel or distance-decay functions. Critically, the distance-weighting function ϕ is distinct from the concept of *distance* (D), itself, which could be measured in Euclidean/geodesic distance, minutes of congested travel time, meters traveled along the sidewalk, or some generalized measure of utility. Separating these two concepts allows us to consider alternative distance metrics distinctly from alternative decay functions. The local environment for a given feature y at location i can then be measured by its *spatial lag*, SL , defined as

$$SL_i = \sum_j w_{ij} y_j . \quad (2)$$

In the spatial econometrics literature, it is common to exclude the diagonal elements from W to differentiate between focal effects and spatial spillovers in regression models, but when the diagonal is filled, then SL_i becomes a consummate measure of the local environment at location i . To compute the spatial multigroup information theory index \tilde{H} , we first calculate local spatially-weighted population proportions as

$$\tilde{\pi}_{im} = \frac{SL_{im}}{\sum_{m=1}^M SL_{im}} . \quad (3)$$

The density at location i is

$$\tilde{\tau}_i = \frac{\sum_{m=1}^M SL_{im}}{\sum_{m=1}^M \sum_{i=1}^I SL_{im}} . \quad (4)$$

The entropy of the local environment at each location \tilde{E}_i is

$$\tilde{E}_i = - \sum_{m=1}^M (\tilde{\pi}_{im}) \log_M(\tilde{\pi}_{im}) . \quad (5)$$

where M indicates the number of groups in the population. Finally,

$$\tilde{H} = 1 - \frac{1}{TE} \sum_i \tilde{\tau}_i \tilde{E}_i \quad (6)$$

where \tilde{H} is the spatial information theory index defined by Reardon and O’Sullivan (2004), T is the total population of the region, and E is the entropy of the region’s total population

$$E = - \sum_{m=1}^M (\pi_m) \log_M (\pi_m). \quad (7)$$

We perform all calculations using the open-source Python package *segregation* (Cortes *et al.* 2020), distributed as part of the Python Spatial Analysis Library (PySAL) (Rey, Anselin, *et al.* 2021)

Assessing Difference Between Distance Metrics

To understand the implications of different parameterizations of space, we use block group-level data from the US Census American Community Survey (ACS) 5-year sample (2013-2017) with four mutually-exclusive racial groups (non-Hispanic white, non-Hispanic Black, Hispanic, and Asian). Our sample contains data for 380 metropolitan Core Based Statistical Areas (CBSAs) in the United States. Block Groups are the smallest geographic unit for which racial and ethnic data are available in the ACS. To compute Euclidean-based spatial segregation measures, our distances are measured between block group centroids; to compute network-based spatial segregation measures, we first attach the block group centroids to the nearest intersection in the travel network, then compute the shortest network-based path between each pair of observations

Our data on street networks is collected from OpenStreetMap and the shortest network path is computed using the Python package *pandana* (Foti *et al.* 2012). To operate efficiently on metropolitan-scale street networks, the *pandana* package relies on a graph pre-processing technique known as contraction hierarchies that simplifies the computation by removing inconsequential nodes from consideration during the routing algorithm (Geisberger *et al.* 2012). Adopting this heuristic provides a massive computational boost, allowing the shortest-path algorithm to perform quickly, even with metropolitan-scale networks. This technique allows us to examine all metropolitan CBSAs in the country, comprising an analysis that includes tens of millions of street intersections.

Constructing Comparable Indices

In each metropolitan region, we proceed by creating two different spatial weights matrices by varying the way distance is measured between observations. In both matrices, the proximity-weighting function ϕ is a simple linear decay (triangular kernel) encoding a spatial weight that decreases with distance up to a threshold of two kilometers, outside of which observations no longer have an effect, (that is, $r = 2000$):

$$\phi = \begin{cases} 1 - \left(\frac{d_{ij}}{r}\right), & \text{if } d_{ij} \leq r \\ 0 & \text{otherwise.} \end{cases} \quad (8)$$

Between the two W matrices, however, we vary the input distance matrix D , between two concepts, Euclidean distance (W_{euc}) and network distance (W_{net}), where network distance is defined as the shortest path along the pedestrian transportation network. In both matrices the diagonal is set to one, indicating that there is no spatial discount for the value located at observation i . Using these weights matrices W_{net} and W_{euc} to build local environments for each metropolitan region in Equation 1 propagates the two constructs through Equations 2, 3, 4, 5, 6, yielding two segregation measures \tilde{H}_{net} , \tilde{H}_{euc} and, implicitly, a difference between the two, $\Delta_{\tilde{H}} = \tilde{H}_{net} - \tilde{H}_{euc}$. The relative difference between segregation measures is the difference divided by the Euclidean measure: $\Delta_{pct} = \frac{\Delta_{\tilde{H}}}{\tilde{H}_{euc}}$.

Inferential Framework

We assess the importance of considering network distance in segregation measurement by adopting the inferential framework outlined in Rey, Cortes, *et al.* (2021) and Cortes *et al.* (2020). The framework leverages a computational approach to statistical inference using random labelling to compare the observed difference between the two segregation measures (network versus Euclidean) to a counterfactual distribution of differences generated from the same data. More specifically, the measures \tilde{H}_{net} , \tilde{H}_{euc} and $\Delta_{\tilde{H}}$ are computed and recorded for each metro region. As a result of this process, two “spatialized” versions of the metropolitan demographic composition are created, with one dataset representing Euclidean distances and the other representing network-based distances.

We then create two synthetic datasets by pooling the input units from both original datasets and reassigning them at random. For each block-group, we randomly reassign the labels (*net*, *euc*) to the observed spatial lags from Equation 2. Once all units have been assigned to a group, the segregation measures are re-computed and their difference taken. This process is repeated 10,000 iterations. By comparing the observed difference in the two segregation measures against a distribution of differences generated via synthetic datasets, we are able to develop inferential statistics using a conventional t -test. Our test, in this case, adopts the null hypothesis that distances come from a common distribution and thus the expected difference in the segregation measures is 0. The p values represent probability that, under the null, a simulated difference is greater than than the observed difference $\Delta_{\tilde{H}}$.

Network Distance is an Important Consideration

Although the Pearson correlation between planar and network based segregation measures is $\rho = 0.987$, our results provide clear evidence that the choice of appropriate distance metric plays an important role in the computation of a spatial segregation index. We highlight this result using the fact that applied segregation research often uses ordinal rankings to describe and compare the magnitude of segregation across a set of places. While still high, the *rank correlation* between the two measures is considerably lower at $\tau = 0.90$. Substantively, this means that an analysis of segregated metropolitan regions will result in different conclusions regarding the “most segregated” places, depending on which distance measure is employed. A visual comparison of the top 15 most segregated metros is

provided in Figure 2, demonstrating how different places exchange ranks, and Figure S3 in the supplementary material portrays the relationship between segregation measured using the two different distance metrics for the sample CBSAs.

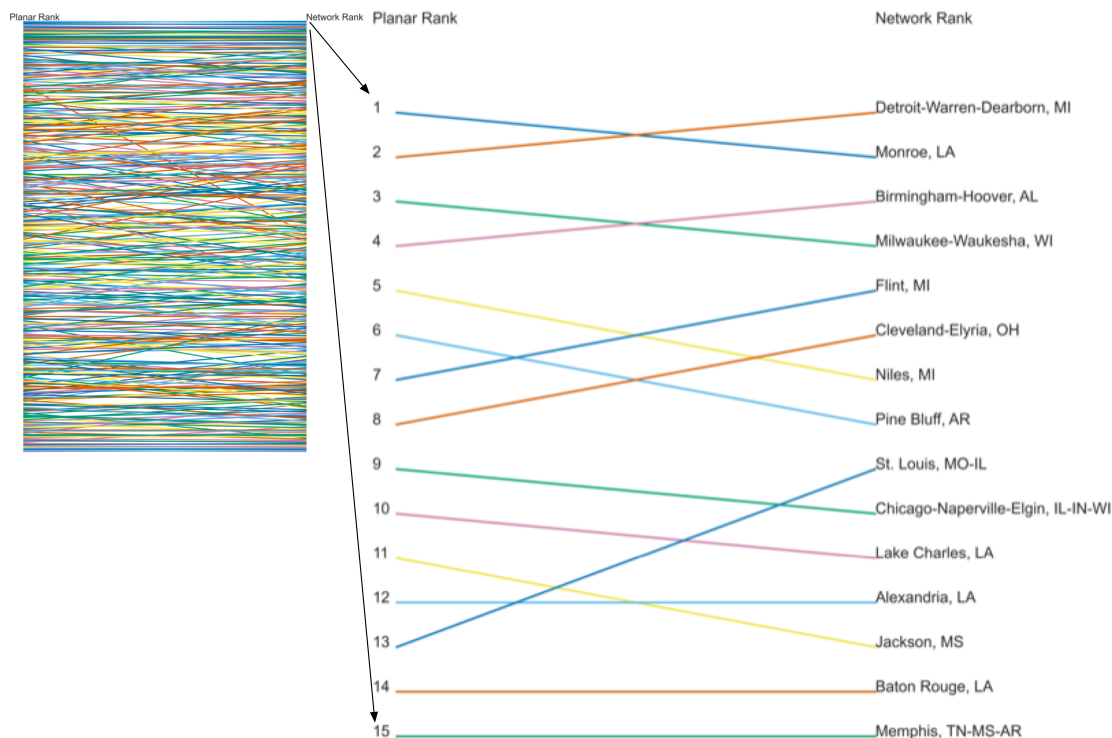


Figure 2: Planar vs. Network Segregation Rankings

When measured in absolute terms, essentially every metropolitan region exhibits higher segregation when measured according to network distance than by pure Euclidean distance³, with only four exceptions (none of the four cases are significantly different from a random pooling of the same data). Among the 380 CBSAs in our dataset, 25.3% have a difference between Euclidean and network-based segregation measures that is significant at the $\alpha = 0.05$ level, and 14.2% of the CBSAs are significant at the $\alpha = 0.01$ level. Descriptive statistics of the differences between segregation measures in each metro are shown in Table 1, and a list of the 54 CBSAs significant at the one percent level are listed in Table S1 in the supplementary material. Among these 54 CBSAs, eight metros are located in California—twice the number of the next-most prevalent state (Texas).

The distributions of both $\Delta_{\tilde{H}}$ and Δ_{pct} are normally-shaped with respective means of 0.029 and 0.198 respectively. While the absolute difference between the two segregation measures in each CBSA can appear small, the relative difference is often reasonably large, with the network-based segregation measure approximately 20% higher than the Euclidean-based measure on average. The largest relative difference gets as high as 69% (Carson City, NV), and the smallest differences are zero (Hat-

³For each CBSA in our sample, our Euclidean distances are based on UTM coordinate systems, with each region's data projected into its appropriate UTM zone.

Table 1: Descriptive Statistics for Segregation Differences

	\tilde{H}_{euc}	\tilde{H}_{net}	$\Delta_{\tilde{H}}$	Δ_{pct}
count	380.000	380.000	380.000	380.000
mean	0.178	0.207	0.029	0.198
std	0.077	0.078	0.013	0.113
min	0.051	0.070	-0.053	-0.204
25%	0.114	0.141	0.023	0.118
50%	0.172	0.205	0.029	0.184
75%	0.224	0.254	0.036	0.260
max	0.454	0.489	0.077	0.694

tiesburg, MS, Longview, TX, Rocky Mount, NC, and California-Lexington Park, MD).

NETWORK CHARACTERISTICS AND SEGREGATION DIFFERENCES

Metropolitan Travel Infrastructure as a Network Graph

The travel infrastructure in a metropolitan region serves as its skeleton for both urban development and social interactions. For decades, scholars have worked to quantify the aspects of urban form that help explain behaviors such as travel mode choice (Crane 2000, Clifton *et al.* 2008, Ewing and Handy 2009, Ewing and Cervero 2010). A recent evolution of this work is the conception of a travel network as a formal graph structure (Boeing 2018a, 2018b, Fleischmann 2018, Araldi and Fusco 2019, Dibble *et al.* 2019, Fleischmann *et al.* 2021), and a set of software tools that facilitate its analysis as such (Boeing 2016, Fleischmann 2019). Understanding the travel network as a topological graph provides a different picture of its accessibility structure and the way it facilitates interaction among residents (Levinson *et al.* 2017). Here our goal is to use these graph topology metrics to explain the variation we observe in $\Delta_{\bar{H}}$.

Measuring Graph Structure

We use the Python packages OSMNx (Boeing 2016) and Momepy (Fleischmann 2019) to create measures of the pedestrian travel network collected from OpenStreetMap. The “pedestrian network” in this case includes all paths that are available to pedestrians (including pathways) but could exclude some unofficial trails or commonly-used passages⁴ Together, these measures provide a summary of the morphological properties of the travel graph structure, and are described in Table 2, where e indexes edges/streets and v indexes nodes/intersections inside a region r . In addition to simple measures like the total length and density of streets, the count and density of intersections, and the proportion of intersections at different levels of throughput, we focus in particular on three measures of the graph structure: cyclomatic complexity, meshedness, and circuitry. In theory, all three measures should be related to the observed difference in segregation when measured in network distance versus Euclidean distance. All else equal, the difference should be smaller when: cycloymatic complexity and meshedness are higher, and when circuitry is lower. Each of these conditions should, in theory, lead to greater flow along the network and a better approximation of unconstrained Euclidean travel.

Table 2: Network Topology Metrics

variable	description	formula
Street segments	Set of street segments in the network	E
Intersections	Set of intersections in the network	V
street-segment-count	Count of street segments in graph	$n_e = E $

Continued on next page

⁴For a complete list of tags used to query the overpass API, see the osmnet software package <https://github.com/UDST/osmnet>

Table 2: Network Topology Metrics

variable	description	formula
intersection-count	Total Intersections in the graph	$n_v = V $
streets-per-node-avg	Average streets per node	$\frac{n_e}{n_v}$
street-length-total	Total length (meters) of streets in graph	$\sum_{uv}^E \text{length}(e_{uv})$
street-length-avg	Average street length	$\sum_{uv}^E \text{length}(e_{uv}) \left(\frac{1}{n_e}\right)$
street-density-km	Street density (per km)	$\frac{n_e}{\sum \text{sqmi}_r}$
self-loop-proportion	Proportion of edges where node u to node v where u equals v	$ E_{\text{self}} \left(\frac{1}{n_e}\right)$, $E_{\text{self}} = \{e \in E \mid e_{uv} = e_{vu}\}$
circuitry-avg	Ratio of edge lengths to straight-line distances between edge endpoints	$\frac{\sum^E \text{length}(e_{uv})}{\sum^E \text{distance}(e_u, e_v)}$
intersection-density-km	Total Intersections per km	$\frac{n_v}{\sum \text{sqmi}_r}$
k-avg	Average node degree	$\sum^V \text{deg}(v) \left(\frac{1}{n_v}\right)$
node-props-dead-end	Proportion of nodes ending in dead end	$ V_2 \left(\frac{1}{n_v}\right)$, $V_2 = \{v \in V \mid \text{deg}(v) = 2\}$
node-props-3way	Proportion of 3-way intersections	$ V_3 \left(\frac{1}{n_v}\right)$, $V_3 = \{v \in V \mid \text{deg}(v) = 3\}$
node-props-4way	Proportion of 4-way intersections	$ V_4 \left(\frac{1}{n_v}\right)$, $V_4 = \{v \in V \mid \text{deg}(v) = 4\}$
cyclomatic	Number of primary loops in the network.	$n_e - n_v + 1$
meshedness	Ratio of faces in the network to the max possible loops in an equivalent network	$\frac{n_e - n_v + 1}{2n_v - 5}$
gamma	Number of edges divided divided by 3 times (nodes minus 2)	$\frac{n_e}{3(n_v - 2)}$
edge-node-ratio	Ratio of streets to intersections	$\frac{n_e}{n_v}$

Cyclomatic complexity can be viewed as a measure of the network’s redundancy, and its ability to provide alternative passages when a given route is blocked. According to Bourdic *et al.* (2012, p. 599), “the cyclomatic number represents the number of primary loops in the network. The greater the number of loops, the greater the number of possible routes in the city... it is more efficient to propose a multiplicity of smaller roads so users can choose and spread over these paths, which are ultimately better suited to the variety of their destinations. The cyclomatic number refers to this multiplicity of loops that increase the number of possible paths. In a public transport network with a high cyclomatic number, a failure in one station will not freeze an entire zone”. As such, we would expect that an increase in cyclomatic complexity would reduce $\Delta_{\bar{H}}$, as more routes are available to provide a short route between two destinations.

The meshedness coefficient is “based on the notion of circuits (or faces), network regions enclosed by loops of linked edges and nodes (analogous to an urban block surrounded by streets) that provide alternate movement routes” (Feliciotti 2018). Meshedness is the “ratio of the number of faces in the network to the maximum possible number of loops in an equivalent network with the same number nodes” (Fleischmann *et al.* 2022). Buhl *et al.* (2006) use the meshedness coefficient to assess the connectedness of a graph, and whether its configuration is closer to a tree-like network or to a maximally connected grid. As Feliciotti (2018) describes, “in strictly tree-like networks, origins and destinations are only linked via a single path, which means that users have only one choice of movement and any point failure in that route would cause major disruption on performance. In turn, grid-like networks provide many ways to get to a same place, greater choice for the user and reduced impact of point failure.”

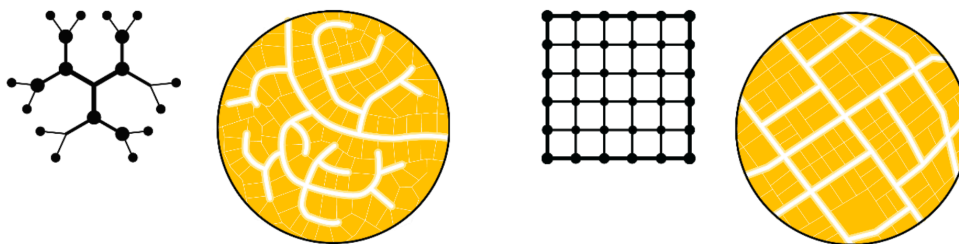


Figure 3: Stylized Depiction of Meshedness by Feliciotti (2018)

In the example of Figure 1, the network in San Clemente Figure 1a is more tree-like than the gridded network in Chicago Figure 1b, indicating that meshedness is higher for Chicago than San Clemente. This distinction is shown similarly in the stylized depiction of meshedness created by Feliciotti (2018) in Figure 3, with the lefthand diagram having a more tree-like structure and thus a lower meshedness coefficient than the diagram on the right. Given the clear difference between Figure 1a and Figure 1b, we would expect that greater meshedness would result in lower $\Delta_{\bar{H}}$ because a denser network results in a further potential travel distance.

Circuitry is a measure of the “windingness” of a city’s streets. It is a ratio of an edge’s network distance to the Euclidean distance between its starting and ending nodes. In stylized terms, it represents the difference between walking between any two intersections and flying between them. For example, a mountain switchback trail would have a higher circuitry measure than a flight of stairs that connected the same two origins and destinations. The former would be easier to traverse because of its lesser slope, but the path would sacrifice greater distance traveled as a result. Here, our measure of circuitry is the average taken over all edges in the network. All else equal, we would expect that a lower circuitry measure would result in a lower $\Delta_{\bar{H}}$ because network distance is closer to Euclidean distance.

Graph Topology and Segregation Differences

We begin with an exploration of correlation among different variables that characterize the graph topological structure, as well as the correlation between $\Delta_{\bar{H}}$ and network structure. Figure 4 shows a “clustermap” of the network topology measures, where the correlation matrix is shaded with green hues indicating positive relationships with purple hues indicating negative relationships, and the intensity denoting the level of correlation. Some network metrics clearly capture the same concept; for example the gamma index is perfectly collinear with the average node degree (k_{avg}), streets per node, and meshedness (given the symmetric nature of the pedestrian network, the average degree is twice the mean streets per node, since each street flows both directions). The meshedness index is also highly correlated with the proportion of four-way intersections, suggesting this component is capturing the network’s throughput.

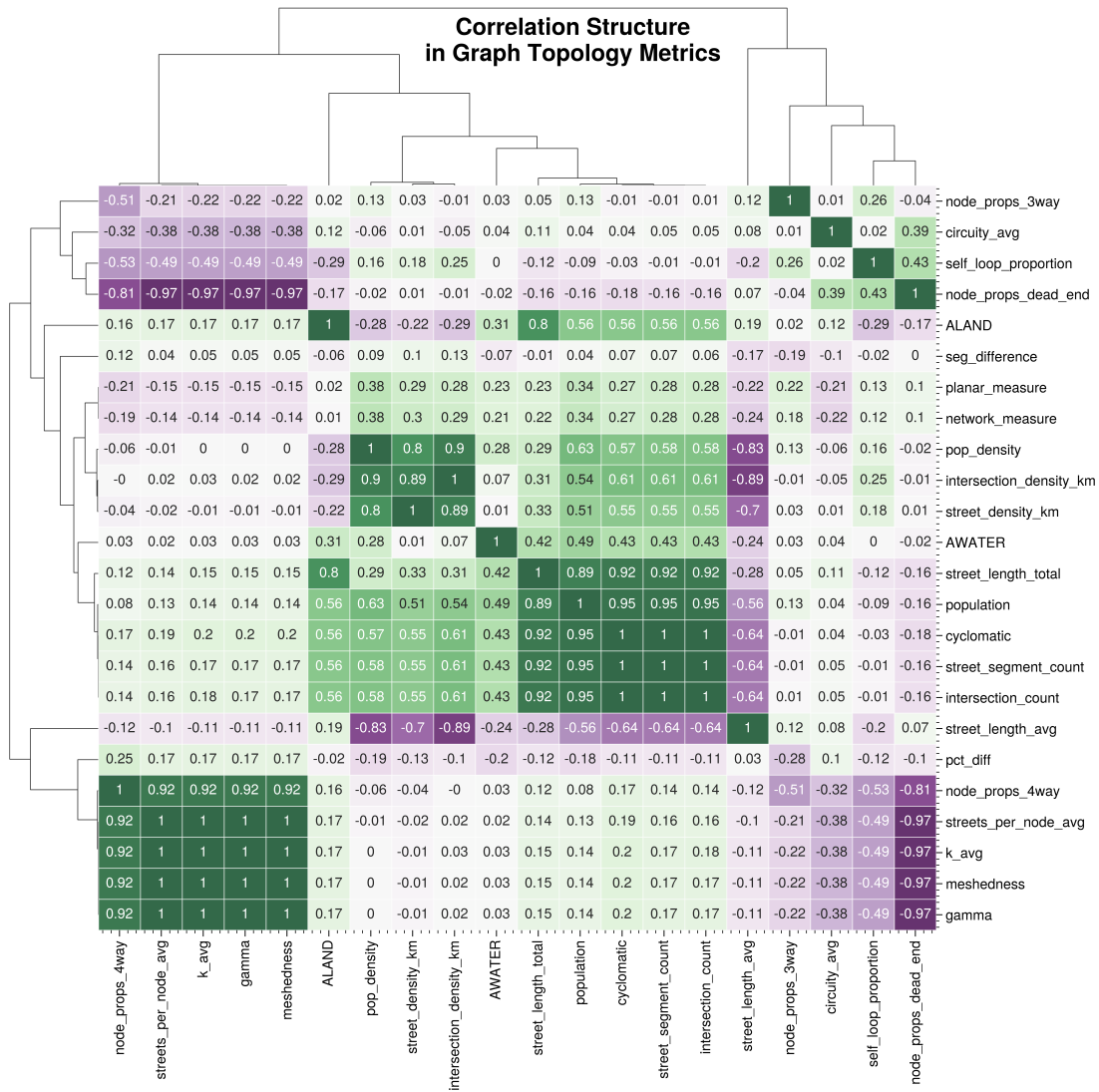


Figure 4: Clustermap of Correlation Structure in Network Metrics

A second group of variables includes population, street length, cyclomatic number, and measures of street and intersection density. This component appears to measure the transportation graph’s complexity and size. The component may also reveal something about agglomeration and self-scaling, as the density measures appear to grow in tandem with size. A final third apparent grouping of variables includes circuitry, and the proportion of self-loops, as well as three-way and dead-end intersections. This component is strongly negatively correlated with the first and appears to indicate network clogging or stoppages. It is interesting to note that circuitry is positively correlated with the proportion of dead-end end streets. Notably each of the three measures under study (cyclomatic complexity, meshedness, and circuitry) each belong to a different component, suggesting that our chosen variables each represent a distinct part of the network structure.

Figure S3 in the supplementary material portrays the pairwise correlations between the percentage difference in the two segregation measures and different properties of the networks in each of the CBSAs. The strongest correlation is between the percentage difference and the size of the difference in segregation. This indicates that the percentage differences are not an artifact of a small denominator problem, whereby low levels of planar segregation would result in even small differences between network and planar based segregation to appear to be large. Focusing on the network properties, as the proportion of 4-way intersections increases the difference between segregation measured using network and planar distances grows. Segregation differences also grow with the average node incidence, street length, edge length, and circuitry of the network. In general, as the size of the network increases, the difference in the segregation measures decreases. The relative differences in segregation measures are negatively associated with the level of segregation in the city.

Modeling the Difference Between Metrics

To understand the importance of graph structure on the difference between segregation measurements we also fit a series of regression models where the difference in segregation is a function of metropolitan network characteristics and population controls. Two models are presented, where the dependent variable Δ is either the observed difference between segregation measures, or the percent difference between the two:

$$\Delta = \alpha + \beta X + \epsilon \tag{9}$$

where α is a constant, X is a subset of the variables described in Table 2, and ϵ is a vector of random errors.

After removing collinear variables such as the share of proportions in different connectivity levels and other constructs well-captured by other variables (see Figure 4), our preferred models include a subset of network topology measures and interactions between cyclomatic complexity and (1) meshedness (2) circuitry. In all specifications, these interactions significantly improved model fit. Moreover, the relationships between variables are generally consistent regardless which dependent

Table 3: Segregation Difference

	$\Delta_{\tilde{H}}$ (1)	Δ_{pct} (2)
ALAND	-0.000 (-0.007, 0.006)	0.090 (-4.125, 4.304)
AWATER	-0.001* (-0.002, 0.000)	-0.441 (-1.143, 0.261)
Intercept	-0.085 (-0.278, 0.109)	-79.192 (-202.584, 44.200)
circuitry_avg	0.653*** (0.163, 1.144)	416.254*** (103.503, 729.005)
cyclomatic	0.132 (-0.346, 0.610)	-8.908 (-313.755, 295.939)
cyclomatic:circuitry_avg	-0.062*** (-0.107, -0.017)	-38.529*** (-67.196, -9.862)
cyclomatic:meshedness	-0.002*** (-0.003, -0.001)	-1.263*** (-2.060, -0.467)
intersection_density_km	-0.152*** (-0.250, -0.055)	-101.501*** (-163.607, -39.396)
meshedness	0.021* (-0.002, 0.043)	15.459** (1.333, 29.586)
planar_measure	0.002 (-0.001, 0.005)	-17.244*** (-19.194, -15.294)
pop_density	0.001 (-0.002, 0.004)	0.245 (-1.900, 2.390)
population	0.001 (-0.004, 0.005)	0.335 (-2.577, 3.246)
self_loop_proportion	-0.001 (-0.006, 0.003)	-0.687 (-3.633, 2.259)
street_density_km	0.149*** (0.051, 0.248)	100.506*** (37.862, 163.149)
street_length_avg	-0.032 (-0.488, 0.425)	-116.565 (-407.718, 174.589)
street_length_total	-0.125 (-0.602, 0.351)	12.341 (-291.562, 316.245)
Observations	369	369
R^2	0.124	0.611
Adjusted R^2	0.089	0.595
Residual Std. Error	0.011(df = 354)	6.981(df = 354)
F Statistic	3.582*** (df = 14.0; 354.0)	39.670*** (df = 14.0; 354.0)
<i>Note:</i>		*p<0.1; **p<0.05; ***p<0.01

variable is used. Right-hand side variables following a Normal distribution are z-transformed and those following a power distribution are transformed via natural logarithm.

Regardless of the chosen dependent variable, the models display similar results, most of which are intuitive. Significant variables include the density of streets and street intersections, network circuitry, and the two interaction terms. As expected, the coefficient for intersection density is negative, suggesting that as the number of intersections per kilometer increases the gap between Euclidean and network-based segregation indices falls. This comports with intuition as greater intersection density leads to a network with greater ability to change direction, and thus a better approximation of unconstrained travel. Circuitry is also positive and significant, suggesting that as streets get more winding and curvilinear, the distance between segregation indices grows. However, the interaction between cyclomatic complexity (a measure of redundancy in the network) and circuitry is negative, which suggests that as the network offers more possible routes between an origin and destination, the effect of circuitry falls. Again, this result is intuitive, as increased cyclomatic complexity offers more opportunities for short-cutting through a circuitous network.

One counterintuitive result is the weakly significant and positive coefficient for network meshedness. Taken at face value, this would suggest that networks with a regular grid pattern increase the distance between segregation measured on the network versus the same data measured on a plane. One possible explanation for this result is an inability of this relatively simple model to account for multiple interactions between meshedness, density, and complexity. While it is possible for a street network to have high intersection density, high street density, and low meshedness (such as a dense but highly dendritic subdivision) such networks are likely comparatively rare in major cities (or are difficult to capture at a metropolitan scale). In such a situation, some variation attributable to meshedness may instead be consumed by the competing coefficients for street density and network density. Exploring the complexity of these relationships is an important avenue for further work.

DISCUSSION

There are two additional parameters worth exploring: the distance-decay function ϕ , and the radius that defines the extent of the local environment r . In this paper we adopt a simple linear decay function but others such as Gaussian and exponential decay functions are applied regularly in both the segregation and spatial interaction literature. Our initial explorations suggest that our findings are robust to the choice of decay function, but future work could explore this issue in greater detail. Further work could also explore the choice of neighborhood radius r . Here we adopt the one-mile radius as a reasonable specification of the neighborhood, but we may obtain different results by choosing a different threshold, particularly when analyzing large heterogeneous networks.

Notably, by varying the r parameter and recalculating the segregation indices presented here it is possible to generate a network-based version of the “multiscalar segregation profile” introduced by Reardon *et al.* (2008), which would provide additional insight into the way that networks may affect multiple scales. In Figure S4 in the supplementary material, we recreate a graph by Roberto (2018)

showing the network-based multiscalar profile for Pittsburgh, PA using our data and methodology. After the critical distance of about one kilometer (which provides travel outside a given blockgroup) the difference between network and Euclidean profiles is roughly constant. Again, this initial exploration suggests our results are likely robust to choice of r , but this finding should be subject to further scrutiny.

There are also other ways researchers could partition or conceptualize the street network graph for further study. In this example, we include a simple set of graph-wide summary measures, e.g. meshedness, average degree, and circuitry. These metrics could also be measured for different “spatial scales” of the network, i.e. different subgraphs (e.g. using the same distance threshold used to define r). Summarizing these measures and using them as input to the regression model would provide a different picture of the relationships; it would also facilitate the inclusion of other commonly used graph metrics, such as closeness centrality or betweenness centrality. The significant interaction effects we uncover between meshedness and cyclomatic complexity and circuitry and complexity also suggest that this is a ripe avenue for further research. In these cases, the significant interaction effects are likely created by heterogeneity in large travel networks, and more refined measures of subgraphs (rather than aggregate summaries of the entire network) may help uncover important localized patterns.

There is also a second issue of spatial scale, which is that here we examine all relationships at a metropolitan scale. Because housing and labor markets are regional in scope, segregation analysis is natural at the metropolitan-level, but adopting such a large scope may obscure important intra-metropolitan variation. For example, metropolitan regions have typically been developed over several distinct time periods, each of which may reflect a particular urban design paradigm or growth management strategy. Since the network measures computed here are averaged over the entire metro region, there may be utility in examining how suburban networks differ from urban ones. Decomposing the urban areas or adopting a multilevel modeling framework could help examine these nested structures.

CONCLUSION

In the segregation literature, the importance of *space* has long been recognized, but a full grasp of its implications still eludes researchers. In this paper, we show that when considering the role of transportation infrastructure in segregation measurement, we obtain substantially different results than classic spatial approaches that adopt Euclidean measurements. More specifically, we show that when ignoring the connectivity of local travel networks, the spatial information theory index \tilde{H} typically underestimates four-group racial segregation by approximately 20%. Using a computational inference framework, we show that this difference is not only substantively meaningful, but also that the difference is large enough that it is unlikely to result from a random process.

Put differently, we show strong evidence that this bias is prevalent in a large share of cases. When examining all metropolitan CBSAs in the United States, between 14% and 25% of the areas show a

statistically significant difference. This result provides new insight into the importance of considering the built environment when conducting spatial analysis in general, and measuring segregation, in particular. By leveraging advances in both network routing algorithms and statistical methods, we analyze metropolitan regions in the United States at a massive scale, finding the shortest routes through millions of street intersections to provide concrete evidence of a widespread phenomenon first suggested by Roberto (2018).

After demonstrating the importance of considering travel infrastructure in segregation measurement, we proceed by measuring the topological characteristics of the pedestrian travel network in each metro region, and assessing their relationships with the observed differences in segregation. We show that many measures of the graph structure are highly intercorrelated, and only a few metrics are necessary for capturing a reasonable picture of the large-scale graph structure. Following, we find that the most important characteristics in the network are intersection density, which reduces the difference between network and Euclidean measurements, and the circuitry of the street network, which increases the difference. Together these findings suggest that network design decisions like ensuring dense and interconnected street grids that adopt straight edges and avoid circuitous patterns can help reduce the segregation measured in metro regions. Nevertheless, the significant interaction effects in the models also suggest more research is necessary to fully understand the effects of heterogeneous network patterns.

In future work, this research could be extended in several directions. One promising avenue is the consideration of alternative impedance measures when calculating shortest-path distances along the travel network. In the present study, we assume a constant rate of travel consistent with the average walking pace, and that impedance is reflected by graph distance alone. Alternative constructs could include elevation along with distance to get a more complete measure of the effort required to traverse by foot or bicycle. Future work could also examine the impacts of other ways to conceive of the “pedestrian” network structure, such as including parks, paths, and trails rather than sidewalks and footpaths included in OSM. Similarly, the travel network could also be extended to include public transportation or (potentially congested) automobile travel. These considerations would require extensive additional data, which may limit the capacity for cross-sectional comparisons, but would also provide insight into alternative concepts of space and distance. They would also provide additional robustness checks against the results here to understand whether the same relationships hold for transit and automobile network, which have considerably different graph properties (Boeing 2018b).

Another important avenue for further work is the blending of multiple graphs for a more complete understanding of multi-contextual segregation. For example children who live in a given neighborhood are simultaneously embedded in local neighborhood contexts, school catchment boundaries, and other local institutions such as religious and community organizations. Each of these contexts have partially-overlapping, occasionally nested, and often imperfectly-defined geographic boundaries, a full synthesis of which requires the development of new methods that integrate across these contexts (Galster 2001, Galster 2019). As one example, Wolf (2021) provides a technique for blending multiple graphs together, one spatial and one aspatial, and similar methods could be pos-

sibly used to integrate multiple contexts. Work along these lines would also help address the call by Reardon and O'Sullivan (2004, p. 156) for metrics that help understand bridges across social networks.

An understated but important contribution of this work is its attempt to bridge the gap between spatial segregation measurement and other areas of spatial analysis. By formulating a spatial segregation index in terms of a spatial lag operator common in spatial econometrics, we hope to foster a greater dialog among researchers in urban social science regarding the most satisfactory ways to encode spatial relationships from both theoretical and methodological perspectives. Given the results presented here, we believe the appropriate operationalization of *space* remains a clear hurdle for understanding social interaction and urban inequality. Thus, we close with a classic reminder from a legendary scholar in spatial analysis, that “it remains for spatial analysts to carefully specify spatial weights matrices so that they truly represent the phenomena being analyzed” (Getis 2009, p. 409). In the context of segregation measurement, it is clear that ignoring intentionally-designed aspects of the built-environment skews our concept of social interaction.

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